



Performing Meta-Analyses in the Case of Very Few Studies

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Outline



- Introduction
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 - Estimation methods
 - Qualitative summary of study results
- Meta-analysis with very few studies
 - Problems, examples
 - Qualitative summary of study results
 - Procedure, examples
- Discussion
- Outlook
 - Beta-binomial Model
 - Bayesian meta-analysis
- Summary
- Conclusion
- References

Poll 1: Continent

Poll 2: Affiliation

Topic for today:



Meta-analyses with very few studies

Studie	Est	SE		Effekt		Effekt		
Studie 1 Studie 2	2.00 2.10	1.00 1.00				2.00 [2.10 [0.04; 0.14;	3.96] 4.06]
DSL				•		2.05 [0.66;	3.44]
KH ohne Ko				•		2.05 [1.41;	2.69]
KH mit Ko			_			2.05 [-6.93;	11.03]
		-20.00	-10.00	0.00	10.00	20.00		

tau^2 PM: 0.000

Methods for evidence synthesis in the case of very few studies

Res Syn Meth. 2018;9:382-392.

Performing Meta-analyses with Very Few Studies

Anke Schulz, Christoph Schürmann, Guido Skipka, and Ralf Bender

In: Evangelou, E. & Veroniki, A.A., Eds.: *Meta-Research: Methods and Protocols*, pp. 91-102. Humana, New York (2022)

Introduction



2 main meta-analytic models:

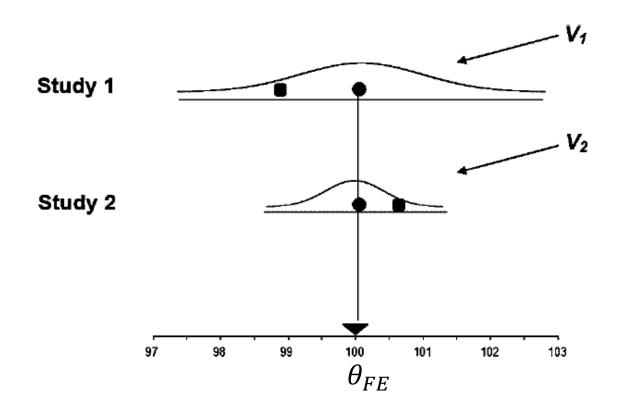
- Model with fixed effect (FEM)
 - Assumption:
 All studies estimate the same effect
 - Better term: "Common-effect model"
- Model with random effects (REM)
 - Assumption:
 The studies estimate different effects
 - For illustrating heterogeneity:
 Prediction intervals (PIs) are useful

Note: There are more models and approaches for meta-analysis. However, in practice, these do not play a major role (see Bender et al., *RSM* 2018).

Meta-analysis: FEM



- $y_i = \theta_{FE} + \varepsilon_i$, $\varepsilon_i \sim N(0, v_i)$, $Var(y_i) = v_i$
- Assumption: All studies estimate the same effect.
- Parameter of interest: **Fixed effect** θ_{FE}

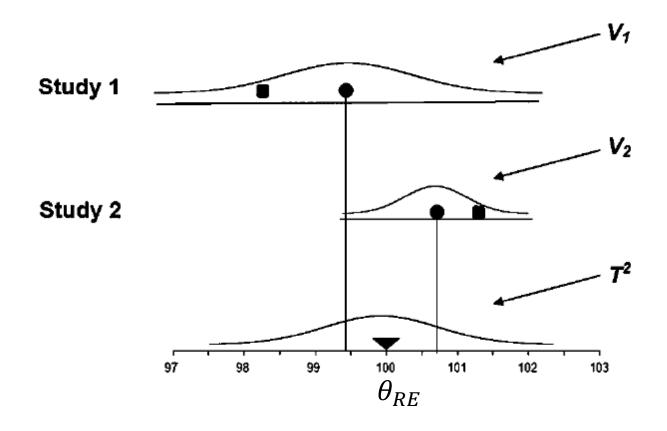


From: Borenstein et al. (2010): *RSM* 1, 97-111.

Meta-analysis: REM



- $y_i = \theta_i + \varepsilon_i$, $\theta_i = \theta_{RE} + \delta_i$, $\varepsilon_i \sim N(0, v_i)$, $\delta_i \sim N(0, \tau^2)$, $Var(y_i) = v_i + \tau^2$
- Assumption: Each study estimates a study-specific true effect.
- Parameter of interest: Expected value θ_{RE} of the effects



From: Borenstein et al. (2010): *RSM* **1**, 97-111.

REM: Prediction interval



Confidence interval (CI):

• 95%-CI:
$$\hat{\theta}_{RE} \pm t_{k-1,1-\frac{\alpha}{2}} \times SE(\hat{\theta}_{RE})$$

- Range, which includes with high certainty (95%) the true effect of the meta-analysis
- Prediction interval (PI):

• 95%-PI:
$$\hat{\theta}_{RE} \pm t_{k-1,1-\frac{\alpha}{2}} \times \sqrt{\tau^2 + Var(\hat{\theta}_{RE})}$$

- Range, which includes with high certainty (95%) the true effect of a single study
- Graphical illustration of heterogeneity in the REM



FEM: Inverse variance (IV)

- Continuous data: Method of inverse variance (IV)
- Point estimate: $\hat{\theta}_{FE} = \frac{\sum_{i=1}^{k} y_i w_{i,FE}}{\sum_{i=1}^{k} w_{i,FE}}$, with $w_{i,FE} = 1/\hat{v}_i$
- 95% CI: $\hat{\theta}_{FE} \pm z_{1-\frac{\alpha}{2}} \sqrt{\frac{1}{\sum_{i=1}^{k} w_{i,FE}}}$, z_q : q-quantile of the normal distribution

FEM: Mantel-Haenszel (MH)

- Binary data: Mantel-Haenszel (MH) method
- Estimation performed by means of the fourfold tables (dependent on effect measure)



REM: DerSimonian & Laird (DSL)

- Historically, the standard approach for RE meta-analysis:
 DSL method (DerSimonian & Laird, CCT 1986)
- Point estimation: $\hat{\theta}_{RE} = \frac{\sum_{i=1}^{k} y_i w_{i,RE}}{\sum_{i=1}^{k} w_{i,RE}}$ with $w_{i,RE} = 1/(\hat{v}_i + \hat{\tau}^2)$
- Point estimation of τ by means of the method of moments
- 95% CI: $\hat{\theta}_{RE} \pm (z_{1-\frac{\alpha}{2}})\sqrt{\frac{1}{\sum_{i=1}^{k} w_{i,RE}}}$, z_{q} : q-quantile of normal distribution
- DSL has been criticized for some time (Cornell et al., AIM 2014)
- DSL ignores the uncertainty of variance estimations
- Cls are frequently too narrow (in the case of few studies)



REM: Hartung-Knapp-Sidik-Jonkman (HKSJ)

- Recommended by the Cochrane Collaboration: HKSJ method (Veroniki et al., RSM 2019)
- Estimation: $\hat{\theta}_{RE} = \frac{\sum_{i=1}^{k} y_i w_{i,RE}}{\sum_{i=1}^{k} w_{i,RE}}$ with $w_{i,RE} = 1/(\hat{v}_i + \hat{\tau}^2)$
- Estimation of τ by means of Paule-Mandel method

• 95% CI:
$$\hat{\theta}_{RE} \pm \left(t_{k-1,1-\frac{\alpha}{2}}\right) \sqrt{\frac{\sum_{i=1}^{k} w_{i,RE}(y_i - \widehat{\theta}_{RE})^2}{(k-1)\sum_{i=1}^{k} w_{i,RE}}}$$
, $t_{m,q}$: q -quantile of t -distribution

- HKSJ holds type 1 error
- Cls frequently very wide (especially in the case of few studies)
- $z_{0.975} = 1.96$, $t_{1;0.975} = 12.7$, $t_{2;0.975} = 4.3$, $t_{3;0.975} = 3.2$, $t_{4;0.975} = 2.8$



REM: Hartung-Knapp-Sidik-Jonkman (HKSJ)

Problems in homogeneous data situations

• 95% CI:
$$\hat{\theta}_{RE} \pm t_{k-1,1-\frac{\alpha}{2}} \sqrt{\frac{\sum_{i=1}^{k} w_{i,RE} (y_i - \hat{\theta}_{RE})^2}{(k-1)\sum_{i=1}^{k} w_{i,RE}}}$$

- SE may be arbitrarily too small and CI too narrow
- Ad-hoc variance correction (Knapp & Hartung, Stat. Med. 2003)

•
$$Var(\hat{\theta}_{RE}) = max \left[\frac{1}{\sum_{i=1}^{k} w_{i,RE}}, \frac{\sum_{i=1}^{k} w_{i,RE} (y_i - \hat{\theta}_{RE})^2}{(k-1)\sum_{i=1}^{k} w_{i,RE}} \right]$$

 Procedure required for the decision whether the ad-hoc variance correction (VC) should be used or not

Qualitative summary of results



Concept of conclusive effects (IQWiG, 2022):

- Data situation, in which an effect can be derived although a meaningful pooled effect estimation is not possible
- No pooled effect estimation when:
 - Heterogeneity is too large
 - Data are insufficient to apply the desired model (REM)

Qualitative summary of results



Concept of conclusive effects (IQWiG, 2022):

- 2 or more estimates are in the same direction
 - Total weight of these studies ≥ 80%
 - ≥ 2 studies are statistically significant
 - Weight of significant studies ≥ 50%
- Moderately and clearly conclusive effects
 - \circ 2 or 3 studies significant \Rightarrow clearly
 - 2 studies significant, 1 study n.s. ⇒ moderately
 - Conclusive situation with 4 studies:
 all 4 studies significant ⇒ clearly
 Null ∉ prediction interval ⇒ clearly
 Null ∈ prediction interval ⇒ moderately



Example 1: Clear data situation

Intervention vs. Kontrolle Endpunkt X Modell mit festem Effekt - Mantel-Haenszel

Studie	Intervention n/N	Kontrolle n/N			RR (95%-KI)			Gewichtung	RR	95%-KI
Studie 1	70/100	00/100		_				13.0	0.79	[0.67, 0.00]
Studie 1		90/100			_			13.8	0.78	[0.67, 0.90]
Studie 2	25/50	32/50	-	•				4.9	0.78	[0.55, 1.10]
Studie 3	100/150	130/150			_			19.9	0.77	[0.68, 0.88]
Studie 4	110/160	140/160			-			21.5	0.79	[0.70, 0.89]
Studie 5	130/180	160/180		-	—			24.5	0.81	[0.73, 0.90]
Studie 6	80/110	100/110			-			15.3	0.80	[0.70, 0.91]
Gesamt	515/750	652/750		•				100.0	0.79	[0.75, 0.83]
			I	1	1					
			0.50	0.71	1.00	1.41	2.00			

Intervention besser

Kontrolle besser

Heterogenität: Q=0.54, df=5, p=0.991, I²=0% Gesamteffekt: Z-Score=-8.37, p<0.001

⇒ Proof of an intervention effect



Example 2: Less clear data situation

Intervention vs. Kontrolle Endpunkt X Modell mit festem Effekt - Mantel-Haenszel

	Intervention	Kontrolle								
Studie	n/N	n/N			RR (95%-KI)			Gewichtung	RR	95%-KI
Studie 1	65/90	80/90						21.4	0.81	[0.70, 0.94]
Studie 2	25/40	30/40			-			8.0	0.83	[0.62, 1.12]
Studie 3	65/80	70/80		-				18.7	0.93	[0.81, 1.06]
Studie 4	20/25	19/25		_	-			5.1	1.05	[0.78, 1.41]
Studie 5	60/130	75/130		-				20.1	0.80	[0.63, 1.01]
Studie 6	80/130	100/130						26.7	0.80	[0.68, 0.94]
Gesamt	315/495	374/495						100.0	0.84	[0.78, 0.91]
			0.50	0.71	1 00	1.41	2.00			

Intervention besser

Kontrolle besser

Heterogenität: Q=5.02, df=5, p=0.413, I²=0.4% Gesamteffekt: Z-Score=-4.17, p<0.001

Poll 3: Significant effect?



Example 2: Less clear data situation

Intervention vs. Kontrolle Endpunkt X Modell mit festem Effekt - Mantel-Haenszel

	Intervention	Kontrolle								
Studie	n/N	n/N			RR (95%-KI)			Gewichtung	RR	95%-KI
Studie 1	65/90	80/90						21.4	0.81	[0.70, 0.94]
Studie 2	25/40	30/40						8.0	0.83	[0.62, 1.12]
Studie 3	65/80	70/80		_	-			18.7	0.93	[0.81, 1.06]
Studie 4	20/25	19/25		_				5.1	1.05	[0.78, 1.41]
Studie 5	60/130	75/130						20.1	0.80	[0.63, 1.01]
Studie 6	80/130	100/130		-				26.7	0.80	[0.68, 0.94]
Gesamt	315/495	374/495		~	-			100.0	0.84	[0.78, 0.91]
				1						
			0.50	0.71	1.00	1.41	2.00			

Intervention besser

Kontrolle besser

Heterogenität: Q=5.02, df=5, p=0.413, I²=0.4% Gesamteffekt: Z-Score=-4.17, p<0.001

⇒ Proof of an intervention effect



Example 3: Unclear data situation

Intervention vs. Kontrolle

Endpunkt X

Modell mit festem Effekt - Mantel-Haenszel

Studie	Intervention n/N	Kontrolle n/N			RR (95%-KI)			Gewichtung	RR	95%-KI
Studie	1014	11/14			1(1((35 /0-1(1)			Cewicitang		3370-101
Studie 1	70/90	75/90		_				22.1	0.93	[0.81, 1.08]
Studie 2	28/40	30/40			-	_		8.8	0.93	[0.71, 1.22]
Studie 3	32/50	35/50			-	-		10.3	0.91	[0.69, 1.20]
Studie 4	45/80	40/80			-			11.8	1.13	[0.84, 1.51]
Studie 5	65/100	70/100			-			20.6	0.93	[0.77, 1.13]
Studie 6	77/100	90/100						26.5	0.86	[0.75, 0.97]
Gesamt	317/460	340/460		ı				100.0	0.93	[0.86, 1.01]
			0.50	0.71	1.00	1.41	2.00			

Intervention besser

Kontrolle besser

Heterogenität: Q=3.41, df=5, p=0.637, I²=0% Gesamteffekt: Z-Score=-1.72, p=0.086

Poll 4: Significant effect?



Example 3: Unclear data situation

Intervention vs. Kontrolle

Endpunkt X

Modell mit festem Effekt - Mantel-Haenszel

	Intervention	Kontrolle								
Studie	n/N	n/N			RR (95%-KI)			Gewichtung	RR	95%-KI
					1					
Studie 1	70/90	75/90		1				22.1	0.93	[0.81, 1.08]
Studie 2	28/40	30/40		· ·	-	- 0		8.8	0.93	[0.71, 1.22]
Studie 3	32/50	35/50			-	-0		10.3	0.91	[0.69, 1.20]
Studie 4	45/80	40/80			-			11.8	1.13	[0.84, 1.51]
Studie 5	65/100	70/100			-			20.6	0.93	[0.77, 1.13]
Studie 6	77/100	90/100			<u> </u>			26.5	0.86	[0.75, 0.97]
Gesamt	317/460	340/460			•			100.0	0.93	[0.86, 1.01]
			1	1	1					
			0.50	0.71	1.00	1.41	2.00			

Intervention besser

Kontrolle besser

Heterogenität: Q=3.41, df=5, p=0.637, I²=0% Gesamteffekt: Z-Score=-1.72, p=0.086

⇒ No proof of an intervention effect



Example 4: REM in clear data situation

Intervention vs. Kontrolle

Endpunkt X

Modell mit zufälligen Effekten - Knapp und Hartung

Studie	Intervention n/N	Kontrolle n/N			RR (95%-KI)			Gewichtung	RR	95%-KI
					111 (33 70 111)			Cementaria		3370111
Studie 1	70/100	90/100			_			15.9	0.78	[0.67, 0.90]
Studie 2	30/40	32/40		· ·	-			7.3	0.94	[0.74, 1.19]
Studie 3	100/150	130/150			_,			18.3	0.77	[0.68, 0.88]
Studie 4	95/160	140/160	-	-				16.4	0.68	[0.59, 0.78]
Studie 5	130/180	160/180		-	-			23.7	0.81	[0.73, 0.90]
Studie 6	80/110	100/110			-			18.4	0.80	[0.70, 0.91]
Gesamt	505/740	652/740		-	-			100.0	0.78	[0.71, 0.86]
95% Prädiktionsintervall					_					[0.67, 0.91]
				1						
			0.50	0.71	1.00	1.41	2.00			

Intervention besser

Kontrolle besser

Heterogenität: Q=6.95, df=5, p=0.224, I²=28.1%

Gesamteffekt: Z-Score=-7.01, p<0.001, Tau(Paule-Mandel)=0.049

⇒ Proof of an intervention effect



Example 5: REM in less clear data situation

Intervention vs. Kontrolle Endpunkt X

Modell mit zufälligen Effekten - Knapp und Hartung

-										
	Intervention	Kontrolle								
Studie	n/N	n/N			RR (95%-KI)			Gewichtung	RR	95%-KI
Studie 1	60/90	80/90		-	_			21.3	0.75	[0.64, 0.88]
Studie 2	25/40	30/40		-				10.1	0.83	[0.62, 1.12]
Studie 3	65/80	70/80		-	-			25.1	0.93	[0.81, 1.06]
Studie 4	20/25	17/25		8	-			8.6	1.18	[0.84, 1.64]
Studie 5	60/130	75/130		-				14.0	0.80	[0.63, 1.01]
Studie 6	80/130	100/130		-				21.0	0.80	[0.68, 0.94]
Gesamt	310/495	372/495						100.0	0.85	[0.74, 0.98]
95% Prädiktionsintervall										[0.65, 1.11]
			0.50	0.71	1.00	1.41	2.00			

Intervention besser

Kontrolle besser

Heterogenität: Q=8.58, df=5, p=0.127, I²=41.7%

Gesamteffekt: Z-Score=-2.90, p=0.034, Tau(Paule-Mandel)=0.088

Provided there is sufficient certainty of the study results, the pooled effect estimate indicates **proof of an intervention effect** (on average!).

However, due to heterogeneity, study situations can be expected, in which the intervention has no effect.



Example 6: Clearly conclusive effects

Intervention vs. Kontrolle

Endpunkt X

Modell mit zufälligen Effekten - Knapp und Hartung (zur Darstellung der Gewichte)

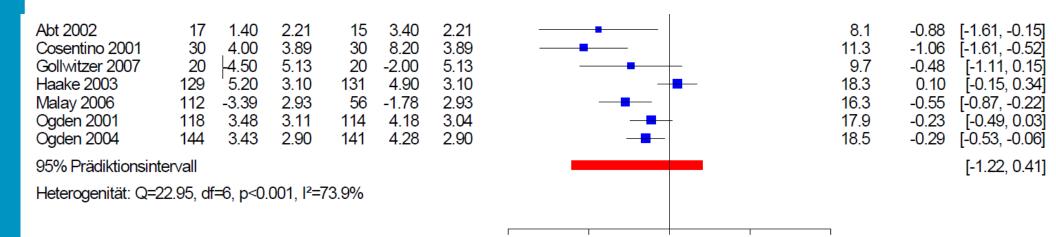
	Intervention	Kontrolle							
Studie	n/N	n/N		RR (95%-KI)		G	Gewichtung	RR	95%-KI
Studie 1	25/90	80/90					15.1	0.31	[0.22, 0.44]
Studie 2	20/40	35/40	_	-			15.4	0.57	[0.41, 0.80]
Studie 3	26/80	75/80					15.8	0.35	[0.25, 0.48]
Studie 4	20/50	40/50		<u> </u>			14.2	0.50	[0.35, 0.72]
Studie 5	50/100	85/100	-	-			20.0	0.59	[0.48, 0.73]
Studie 6	50/130	120/130	-	-			19.6	0.42	[0.33, 0.52]
95% Prädiktionsintervall									[0.24, 0.82]
			0.20 0.45	1.00	2.24	5.00			
			Intervention	n besser Ko	ntrolle besser				

Heterogenität: Q=16.30, df=5, p=0.006, I²=69.3%

Provided there is sufficient certainty of the study results, the clearly conclusive effects indicate proof of an intervention effect (but with an unclear effect size).



Example 7: Moderately conclusive effects



-1.00

FSWT besser

0.00

1 00

Schein besser

2.00

The decision, whether the intervention is beneficial depends on the certainty of the study results.

-2.00

(RCTs with low risk of bias or non-RCTs with high or unclear risk of bias?)



Example 8: No conclusive effects

Intervention vs. Kontrolle

Endpunkt X

Modell mit zufälligen Effekten - Knapp und Hartung (zur Darstellung der Gewichte)

Studie	Intervention n/N	Kontrolle n/N			RR (95%-KI)			Gewichtung	RR	95%-KI
Studie 1	25/90	80/90						16.0	0.31	[0.22, 0.44]
Studie 2	35/40	30/40			 			17.0	1.17	[0.94, 1.44]
Studie 3	60/100	70/100			-			17.0	0.86	[0.70, 1.05]
Studie 4	20/50	40/50		-	_			15.8	0.50	[0.35, 0.72]
Studie 5	90/120	70/120			-			17.2	1.29	[1.07, 1.54]
Studie 6	50/120	110/120		-	-			17.0	0.45	[0.37, 0.57]
95% Prädiktionsintervall			-							[0.15, 3.15]
				1						
			0.10	0.32	1.00	3.16	10.00			

Intervention besser

Kontrolle besser

Heterogenität: Q=107.73, df=5, p<0.001, I2=95.4%

⇒ No proof of an intervention effect

Very few studies (k<5)



Problems with meta-analyses with very few studies (Bender et al., 2018):

- Choice between FEM and REM difficult
- τ cannot be adequately estimated
- DSL-Cls are too narrow
- HKSJ-CIs are wide or even non-informative
- In homogeneous data situations HKSJ-CIs are sometimes too narrow

Example: IQWiG Report A15-25



Belatacept after kidney transplant (2 significant studies)

- Belatacept vs ciclosporin A for prophylaxis of graft rejection in adults receiving a renal transplant
- Endpoint "renal insufficiency in chronic kidney disease stage 4/5"

belatacept vs. ciclosporin A renal insufficiency in chronic kidney disease

	logarithmic					
Study	effect	SE	effect (95% CI)	weight (DSL)	effect	95% CI
BENEFIT BENEFIT-EXT	-0.82 -0.51	0.17 0.13		44.6 55.4	0.44 0.60	[0.32, 0.61] [0.46, 0.78]
DSL			•	100.0	0.52	[0.39, 0.71]
CE IV			•		0.53	[0.43, 0.65]
КН					0.52	[0.07, 3.71]
		0.01	0.10 1.00 10.00 favors belatacept favors ciclosporin A	100.00		

Heterogeneity: Q=2.06, df=1, p=0.151, I²=51.5% Overall effect: Z Score=-4.21, p<0.001, Tau=0.157



- 1) HKSJ over-conservative
- 2) Decision of no added benefit would be critical

Example: IQWiG Report A14-38



Sipuleucel-T in prostate cancer (3 significant studies)

- Sipuleucel-T vs appropriate comparator for asymptomatic or minimally symptomatic metastatic prostate cancer in males
- Endpoint fever

sipuleucel-I vs. comparator fever

	sipuleucel-T	comparator				
Study	n/N	n/N	RR (95% CI)	weight (DSL)	RR	95% CI
IMPACT	99/338	23/168	-	58.9		[1.41, 3.24]
D9901	28/82	2/45		17.6		[1.92, 30.77]
D9902A	19/65	3/31	-	23.5	3.02	[0.97, 9.44]
DSL	146/485	28/244	-	100.0	2.91	[1.50, 5.65]
CE IV			•		2.44	[1.68, 3.55]
КН					2.88	[0.70, 11.92]
			0.01 0.10 1.00	10.00 100.00		
			favors sipuleucel-T favo	ors comparator		

Heterogeneity: Q=3.29, df=2, p=0.193, l²=39.1% Overall effect: Z Score=3.15, p=0.002, Tau=0.388

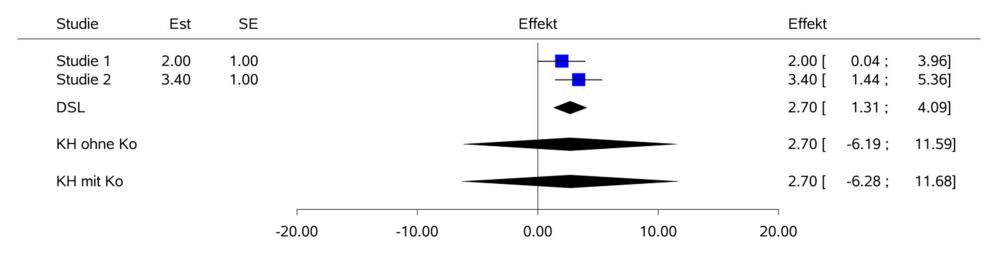


Even in the case of 3 studies HKSJ method over-conservative

Artificial examples



Ad-hoc variance correction (VC) for HKSJ



tau^2 PM: 0.000

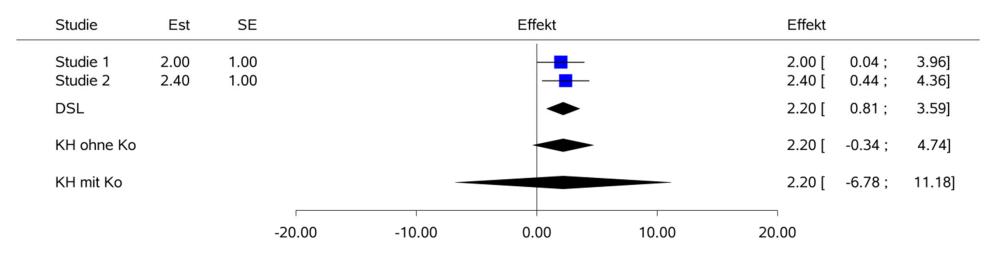


HKSJ over-conservative Ad-hoc VC not required

Artificial examples



Ad-hoc variance correction (VC) for HKSJ



tau^2 PM: 0.000



HKSJ CI-width decreases with increasing homogeneity Is the use of ad-hoc VC required?

Artificial examples



Ad-hoc variance correction (VC) for HKSJ

Studie	Est	SE		Effekt		Effekt		
Studie 1 Studie 2 DSL	2.00 2.10	1.00 1.00				2.00 [2.10 [2.05 [0.04; 0.14; 0.66;	3.96] 4.06] 3.44]
KH ohne Ko				•		2.05 [1.41;	2.69]
KH mit Ko						2.05 [-6.93 ;	11.03]
		-20.00	-10.00	0.00	10.00	20.00		

tau^2 PM: 0.000



HKSJ-Cl clearly too narrow Variance correction required, but over-conservative



Comparison with DSL to decide whether ad-hoc VC should be used (Schulz et al., 2022)

Procedure in the case of very few studies



- Step 1: Preliminary model choice
 - PICOS framework
 - In general: RE model
 - 2 studies: FE model (studies with identical design)
- Step 2: Evaluation of heterogeneity
 - Too large, unexplained heterogeneity: MA not useful
 - Q-Test, I², visual inspection of forest plot
 - If this is the case: Qualitative summary (QS)
- Step 3: Final model and method choice
 - Strong heterogeneity: Reconsider preliminary choice
 - FE model: IV (continuous) or MH (binary)
 - RE model: HKSJ (if required VC) or QS (comparison with DSL and comparison with QS)

Example: IQWiG Report N16-02



- Use of ad-hoc VC required?
 - Comparison of CIs from DSL and HKSJ
 - O HKSJ-Cl narrower than DSL-Cl ⇒ Use VC

Telemonitoring vs. Control Mortality

Study	Telemonitoring n/N	Control n/N	OR (95% CI)	weight	OR	95% CI
REDUCEhf REM-HF TELECART	7/202 128/824 7/89	9/198 152/826 8/94		5.8 88.9 5.3	0.75 0.82 0.92	[0.28, 2.07] [0.63, 1.06] [0.32, 2.64]
REM - HKSJ	142/1115	169/1118	•	100.0	0.82	[0.74, 0.90]
REM - HKSJ (varia	nce corr.)				0.82	[0.48, 1.39]
REM - DerSimonia	n-Laird				0.82	[0.64, 1.04]
			0.25 0.33 0.50 1.00 2.00 3.00 favors Telemonitoring favors Control	0		

Heterogeneity: Q=0.07, df=2, p=0.965, I²=0%

Overall effect (REM - HKSJ): Z Score=-8.66, p=0.013, Tau(Paule-Mandel)=0



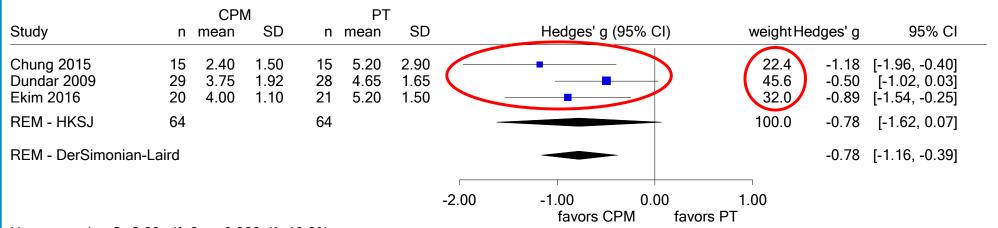
 $HKSJ(VC) \Rightarrow No proof of an effect$

Example: IQWiG Report N16-03



- Is HKSJ informative? Significance of HKSJ vs DSL?
 - O HKSJ-CI wider than the union of study CIs?
 - O HKSJ informative, but n.s., DSL stat. sign. ⇒ QS

Continuous Passive Motion vs. Physical Therapy Pain



Heterogeneity: Q=2.23, df=2, p=0.328, I²=10.2%

Overall effect (REM - HKSJ): Z Score=-3.96, p=0.058, Tau(Paule-Mandel)=0.107



26.01.2023

QS ⇒ Benefit of the intervention (but effect size is unclear)

Example: IQWiG Report N19-01



- Is HKSJ informative? Significance of HKSJ vs DSL?
 - O HKSJ-CI wider than the union of study CIs?
 - O HKSJ informative, but n.s., DSL n.s. ⇒ HKSJ & DSL

Telemedicine vs. Control Mortality

Study	TM n/N	Control n/N	OR (95% CI)	weight	OR	95% CI
IN-TIME TELECART TIM-HF TIM-HF2	10/333 7/89 54/354 61/765	27/331 8/94 55/356 89/773		19.3 12.0 32.7 35.9	0.35 0.92 0.99 0.67	[0.17, 0.73] [0.32, 2.64] [0.65, 1.48] [0.47, 0.94]
REM - HKSJ	132/1541	179/1554		100.0	0.69	[0.35, 1.39]
REM - DerSimonian-Laird					0.70	[0.47, 1.04]
			0.15 0.37 1.00 2.70 favors TM favors Control			

Heterogeneity: Q=6.34, df=3, p=0.096, I²=52.7%

Overall effect (REM - HKSJ): Z Score=-1.68, p=0.192, Tau(Paule-Mandel)=0.318



HKSJ & DSL \Rightarrow No proof of an effect

Discussion



- No satisfactory standard method is currently available to perform meta-analyses in the case of very few studies
- FEM possible in practice, but has limitations
- Therefore, in general, the REM should be used (unless there are clear reasons to justify the use of the FEM)
- Problem: In the case of very few studies, REM frequently has low power and does not yield informative results
- In the case of only 2 studies, the FEM should be used (despite of the general recommendation) unless there are clear reasons against the use of the FEM
- Reason: In situations with only 1 single study, results of this study are interpreted and conclusions are made (in principle, application of the FEM)

Discussion



- In the case of 3-4 studies: REM should be used (unless there are clear reasons to justify the use of the FEM)
- Use of HKSJ (with checks regarding VC and whether the result is informative)
- Application of HKSJ or HKSJ-VC or QS
- For QS:
 - Concept of conclusive effects
 - Prediction intervals
- Other promising possibilities:
 - Beta-binomial model (Felsch et al., BMC-MRM 2022)
 - Bayesian meta-analysis with informative prior for τ
 (Röver et al., RSM 2021; Lilienthal et al., work in progress)

Outlook



Beta-binomial model (BBM)

- Suitable for binary data
- Simulation study by IQWiG in collaboration with Tim Mathes (Göttingen) and Oliver Kuß (Düsseldorf)
- Results (Felsch et al., BMC-MRM 2022):
 - No advantages in the case of 2 studies
 - More power than HKSJ in the case of 3-4 studies



Consideration of inclusion of the BBM in the procedure described before

Outlook



Bayesian meta-analysis

- Required: Slightly informative prior for τ
- Good compromise between DSL und HKSJ
- IQWiG-project in collaboration with Tim Friede and Christian Röver (Göttingen):
 - Derivation of empirical priors for τ from meta-analyses of IQWiG reports (see "A Day with ... SMG" 11.05.2021: https://training.cochrane.org/learning-events/learning-live/day/day-smg)
 - Currently: Estimation of empirical priors for τ by means of the hierarchical Bayes model according to Röver et al. (Stat. Med. 2023, under review)
 - Manuscript in preparation with suggestion of priors for τ for the effect measures RR, OR, HR, SMD (suitable for HTA) (Lilienthal et al., 2023, work in progress)

Summary



Evidence synthesis in the case of very few studies:

- Too large, unexplained heterogeneity: QS
- 2 studies:
 Standard model FEM (IV or MH)
- 3-4 studies:
 - REM with HKSJ or HKSJ-VC (if HKSJ yields useful information)
 - QS (if HKSJ yields no useful information or when DSL stat. sign.)
- 5 studies or more: REM with HKSJ or HKSJ-VC
- Future: BBM and Bayes (with informative prior for τ)

Conclusion



- No satisfactory universal standard method is currently available to perform meta-analyses in the case of very few studies
- Additional approaches (beta-binomial model, Bayes) are under consideration
- The procedure currently used by IQWiG (combination of FEM, REM, QS) represents a feasible approach to perform evidence syntheses with very few studies in practice

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